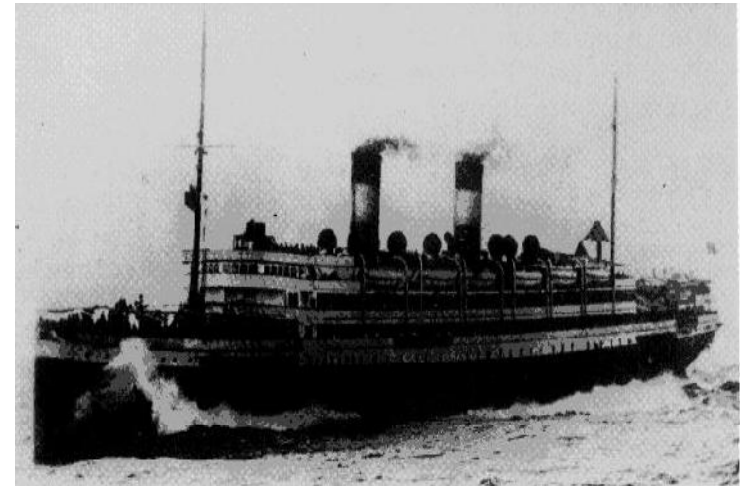
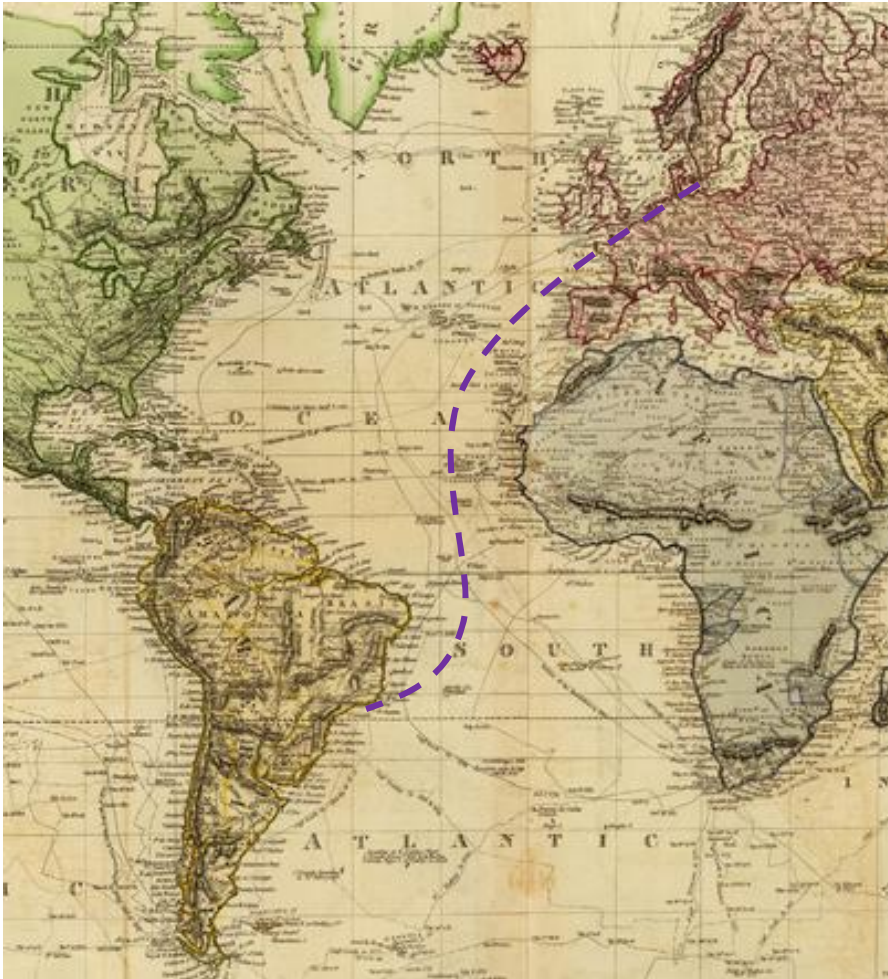


Looking for the right time to shift strategy in the Exploration-Exploitation Dilemma

Filipo STUDZINSKI PEROTTO

Anecdote



XIX Century
Immigrants

Summary

- Exploitation-Exploration Dilemma
- Generalities
- Standard Approaches x Proposed Approach
- Experimental Setting and Results
- Conclusions and Perspectives



Exploration – Exploitation Dilemma



Exploration-Exploitation Dilemma

Should I...



...try something new? or just... enjoy a known pleasure?



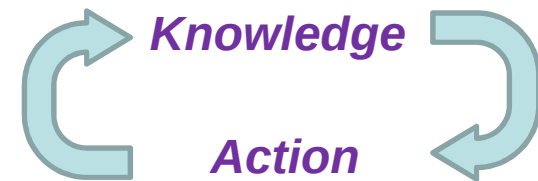
Exploration-Exploitation Dilemma

Any kind of adaptive agent...

(humans, animals, robots, societies, companies, ...)

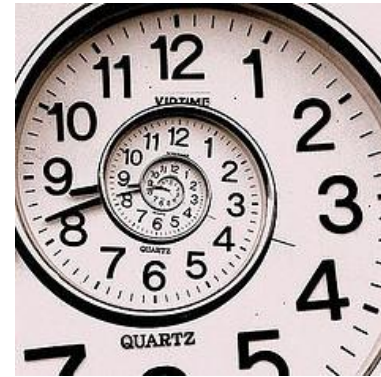
...must perform and learn at the same time.

- how to balance it?
- more knowledge = better performance
- but learning = investment



Exploration-Exploitation Dilemma

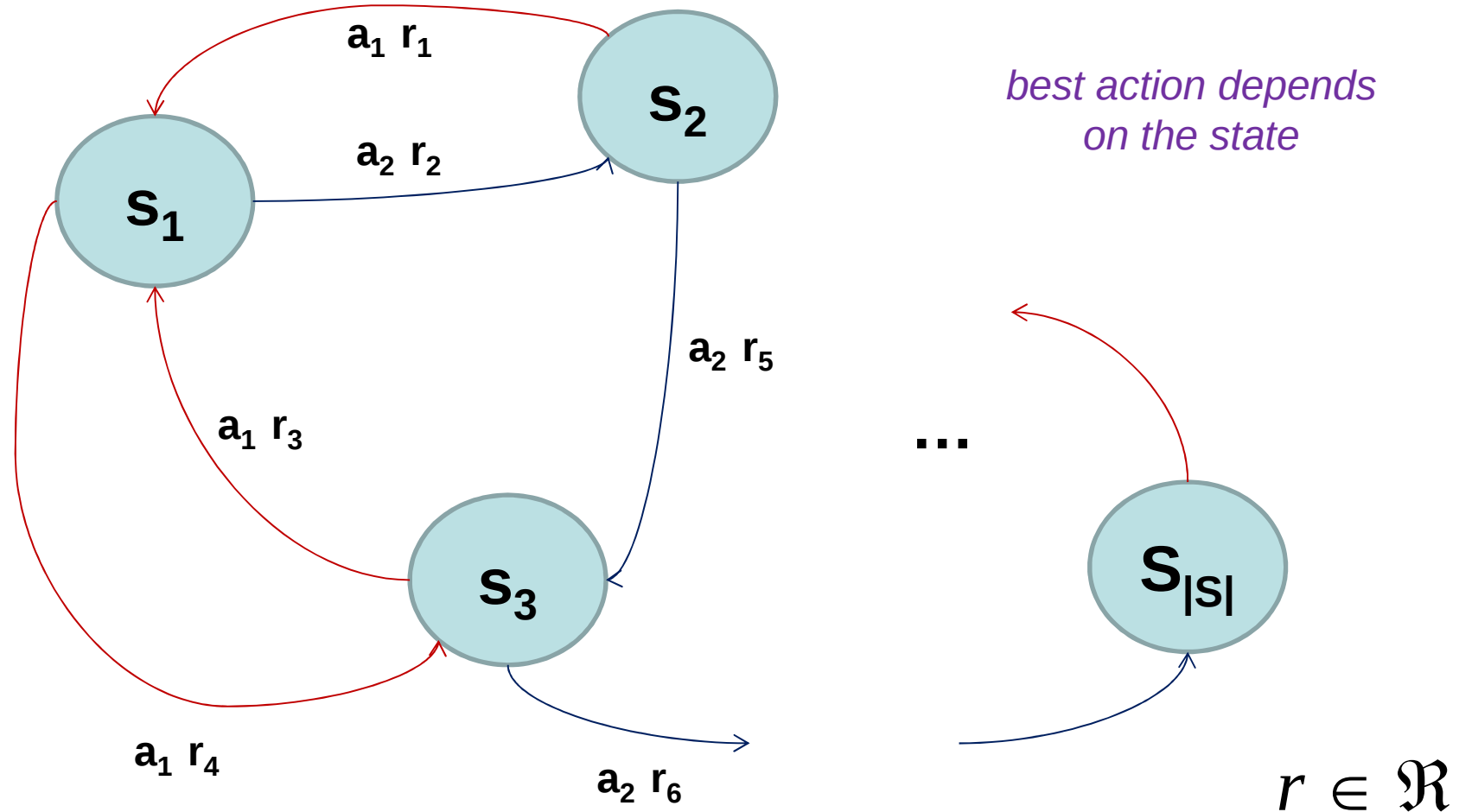
- When to explore ?
- How to explore ?



Generalities



Markovian Decision Process



Markovian Decision Process (MDP)

$\mathbf{S} = \{s_1, s_2 \dots s_{|S|}\}$ set of states

$\mathbf{A} = \{a_1, a_2 \dots a_{|A|}\}$ set of actions

$\mathbf{T} = \Pr (s' \mid s, a)$ transition function

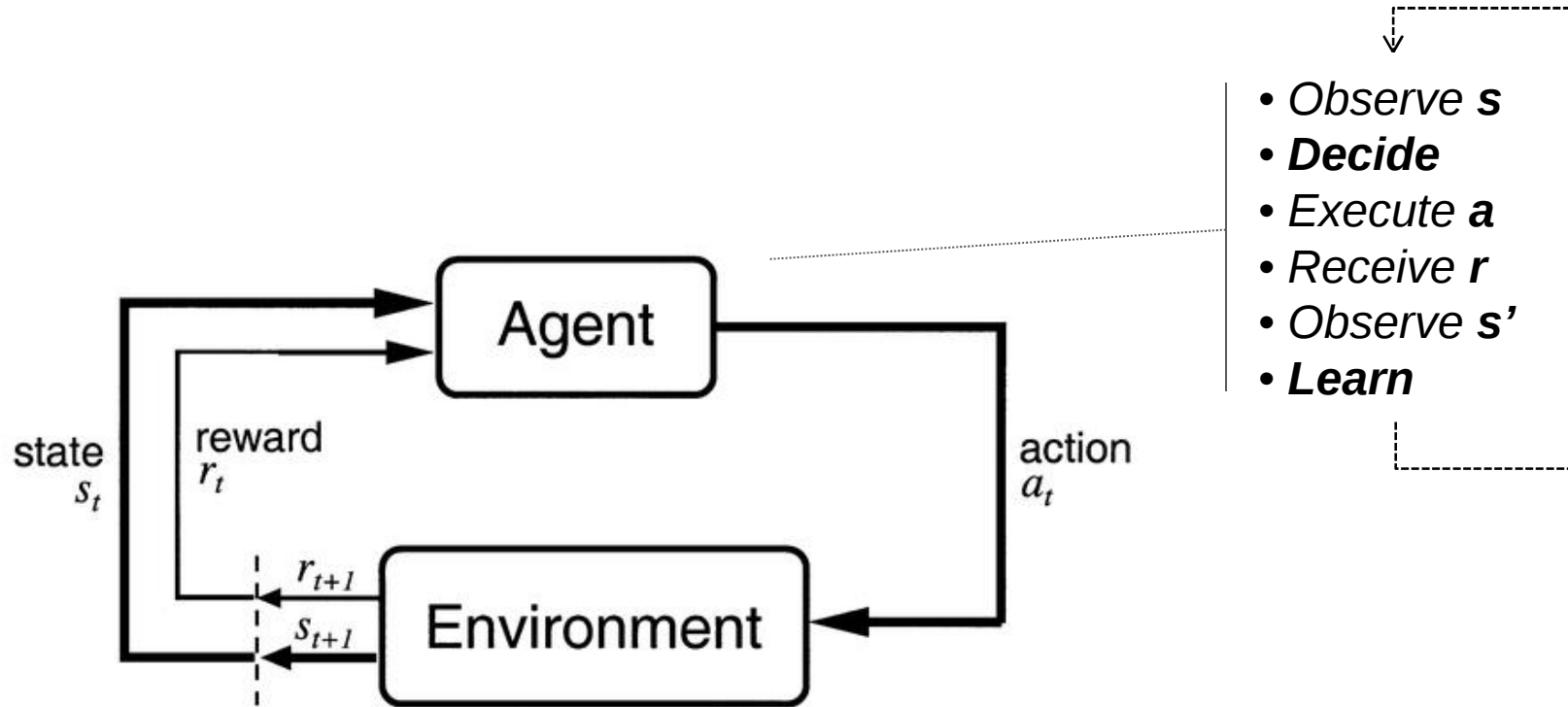
$\mathbf{R} = \Pr (r \mid s, a, s')$ reward function

Solution : a policy of actions $\mathbf{p} : S \rightarrow A$

which maximizes expected future rewards



Reinforcement Learning



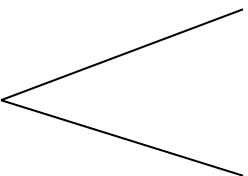
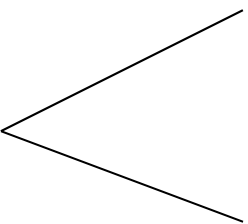
Non-episodic setting : continuous lifetime experience

Agent Lifecycle

- *Observe s*
- ***Decide***
 - *Choose Strategy*
 - *Select Action (from policy)*
- *Execute a*
- *Receive r*
- *Observe s'*
- ***Learn***
 - *Update Models*
 - *Calculate Utility*
 - *Redefine Policy*

*model-based learning

Agent Lifecycle

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 - ***Choose Strategy***
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*model-based learning



Issues

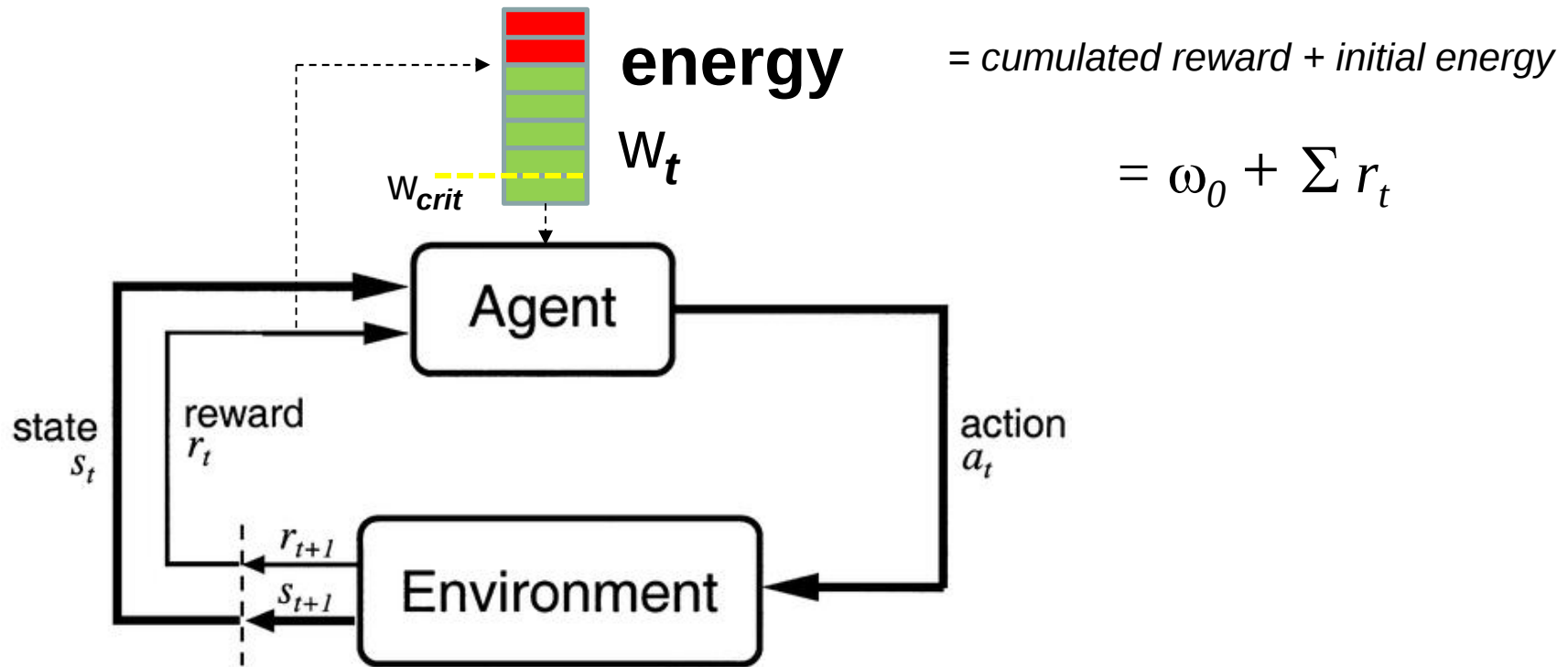


RL with Limited Resources



- How about costs?

Reinforcement Learning **with Energy**



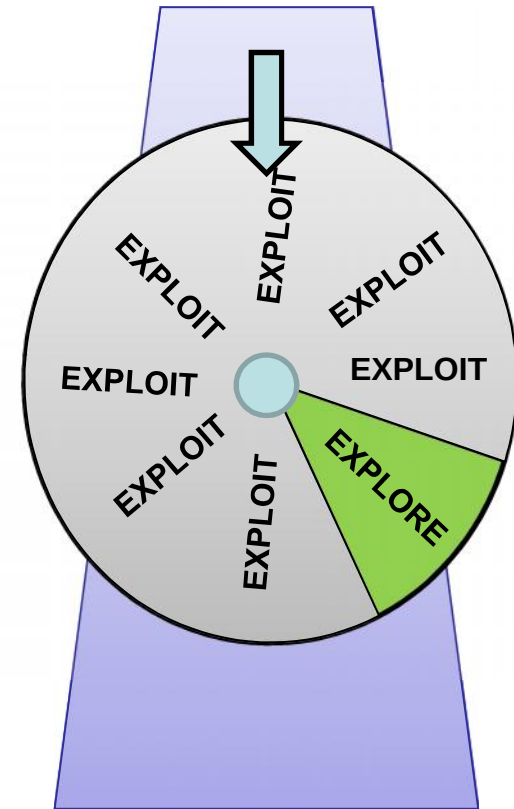
New challenge : managing costs, alert under $\omega_{\min}$

Standard Approaches



Epsilon-Greedy Method

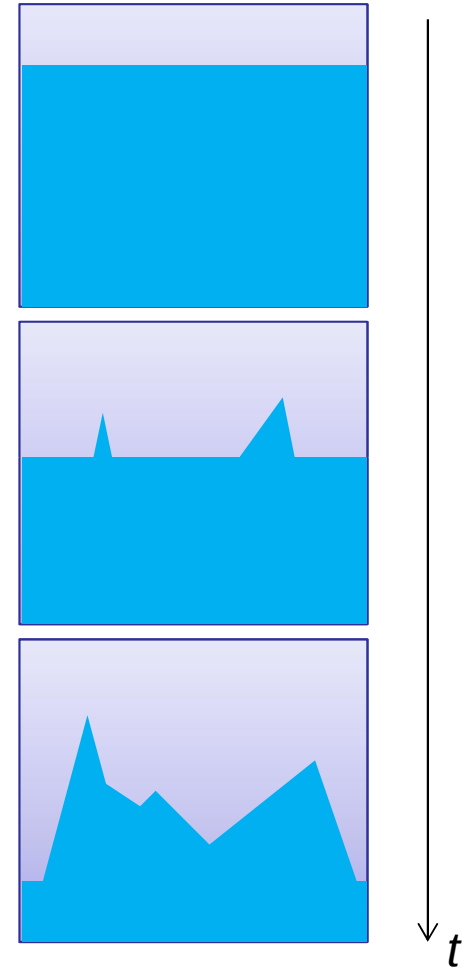
- Choose exploration with probability ϵ
- Choose exploitation with probability $1-\epsilon$



* $\{ \epsilon \in \mathbb{R} \mid 0 \leq \epsilon \leq 1 \}$

Optimism in face of incertitude

- Optimistic initialization
 - Optimistic-greedy
 - R-max
 - $Q_0(s, a) > Q^*(s, a)$
 - $\hat{R}_0(s) > R(s)$
- Exploration bonus
 - UCB
 - Uncertain or infrequent states



How to explore ?

- Undirected :
= Random

“when exploring,
do something unexpected”

→ choose action at random

- Directed :
= Exploration Bonus

“when exploring,
go towards unknown situations”

→ search less visited states

→ or more unpredictable states



Standard Approaches Difficulties

- Random Exploration
 - not very efficient in general
 - not like curiosity
 - can leads the agent to known bad choices
- Epsilon Methods
 - not efficient for sequential problems
- Optimistic Methods
 - efficient exploration
 - but long forced initial training time
 - costs not taken in account

Proposed Approach



Engaged Climber

- Intuition :
 - Choose the strategy (explore / exploit)
 - Stay engaged for a while (until to reach a “peak”)
 - Except in critical situations



Engaged Climber

- 2 Policies :
 - π_R : policy for exploiting
 - π_K : policy for exploring
- 2 Utilities:
 - V_R, Q_R : Exploiting Utility based on reward
 - V_K, Q_K : Exploring Utility based on uncertainty



Engaged Climber

- Parameters :

ξ : time in the current strategy

ξ_{max} : maximum engagement time

r_{peak} : peak reward

ω_{crit} : critical energy level alert

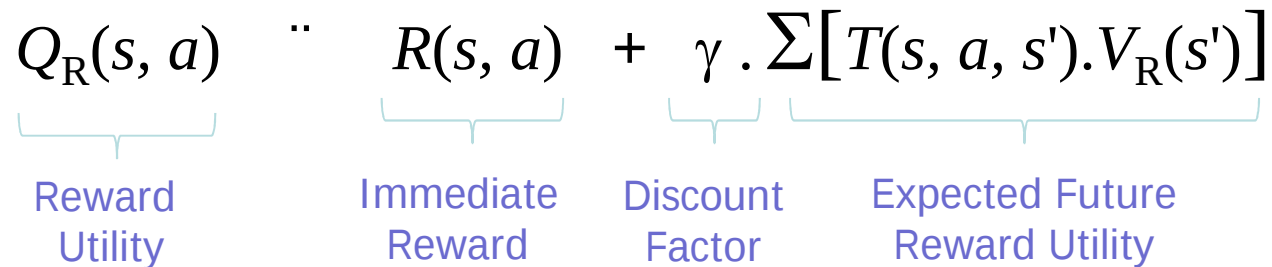
ε : exploration rate



Engaged Climber

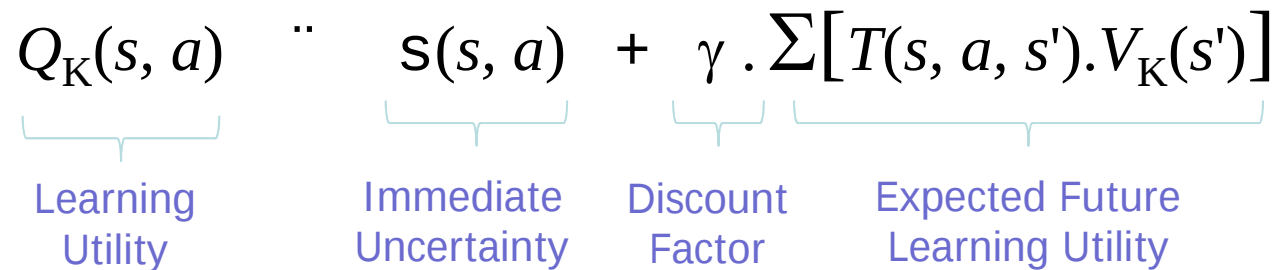
- Update Utilities :

$$Q_R(s, a) \leftarrow R(s, a) + \gamma \cdot \sum [T(s, a, s') \cdot V_R(s')]$$



Reward Utility Immediate Reward Discount Factor Expected Future Reward Utility

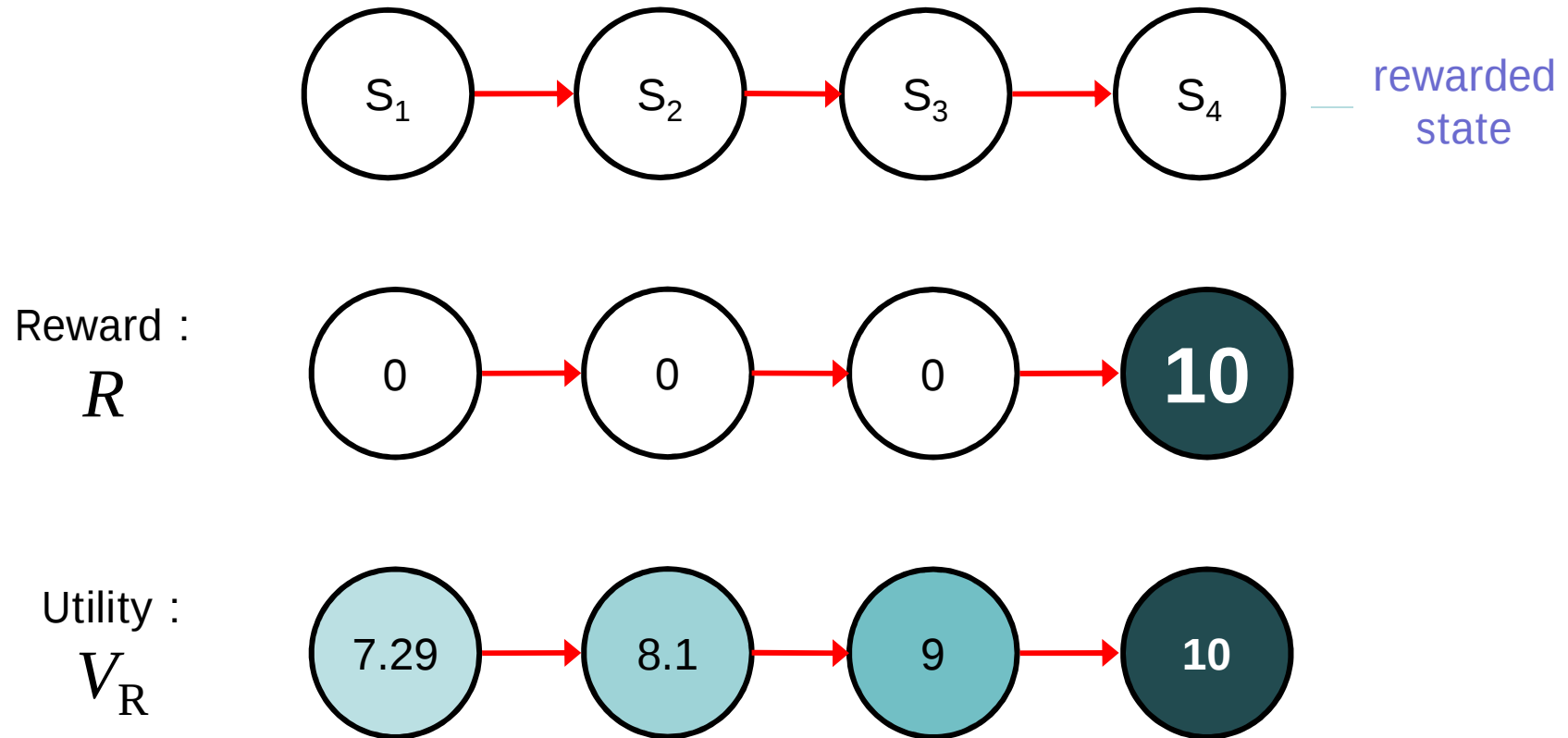
$$Q_K(s, a) \leftarrow s(s, a) + \gamma \cdot \sum [T(s, a, s') \cdot V_K(s')]$$



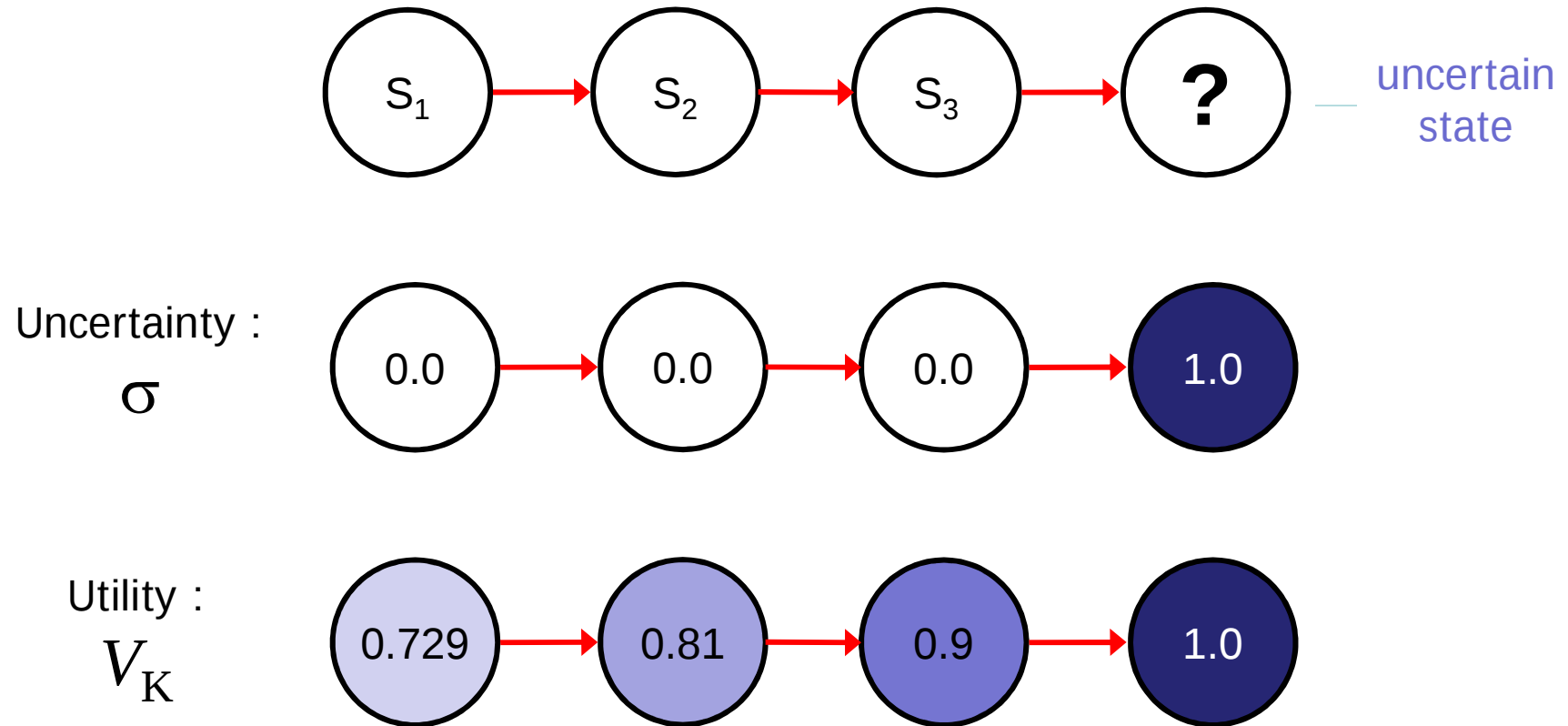
Learning Utility Immediate Uncertainty Discount Factor Expected Future Learning Utility



Reward Utility

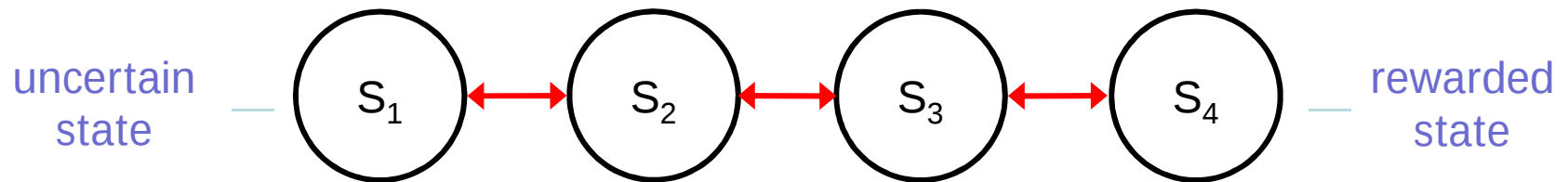
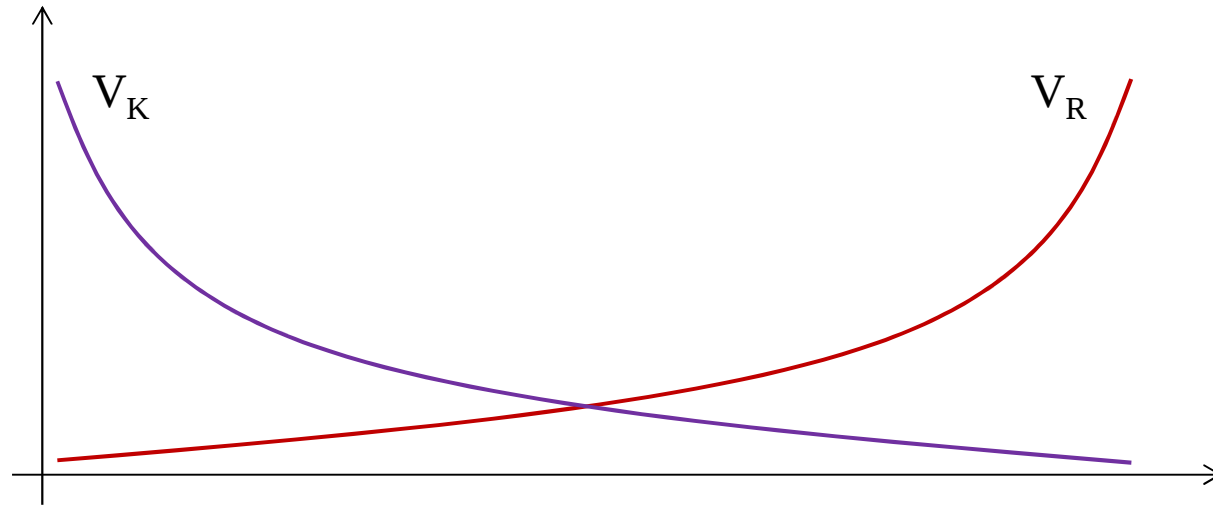


Learning Utility

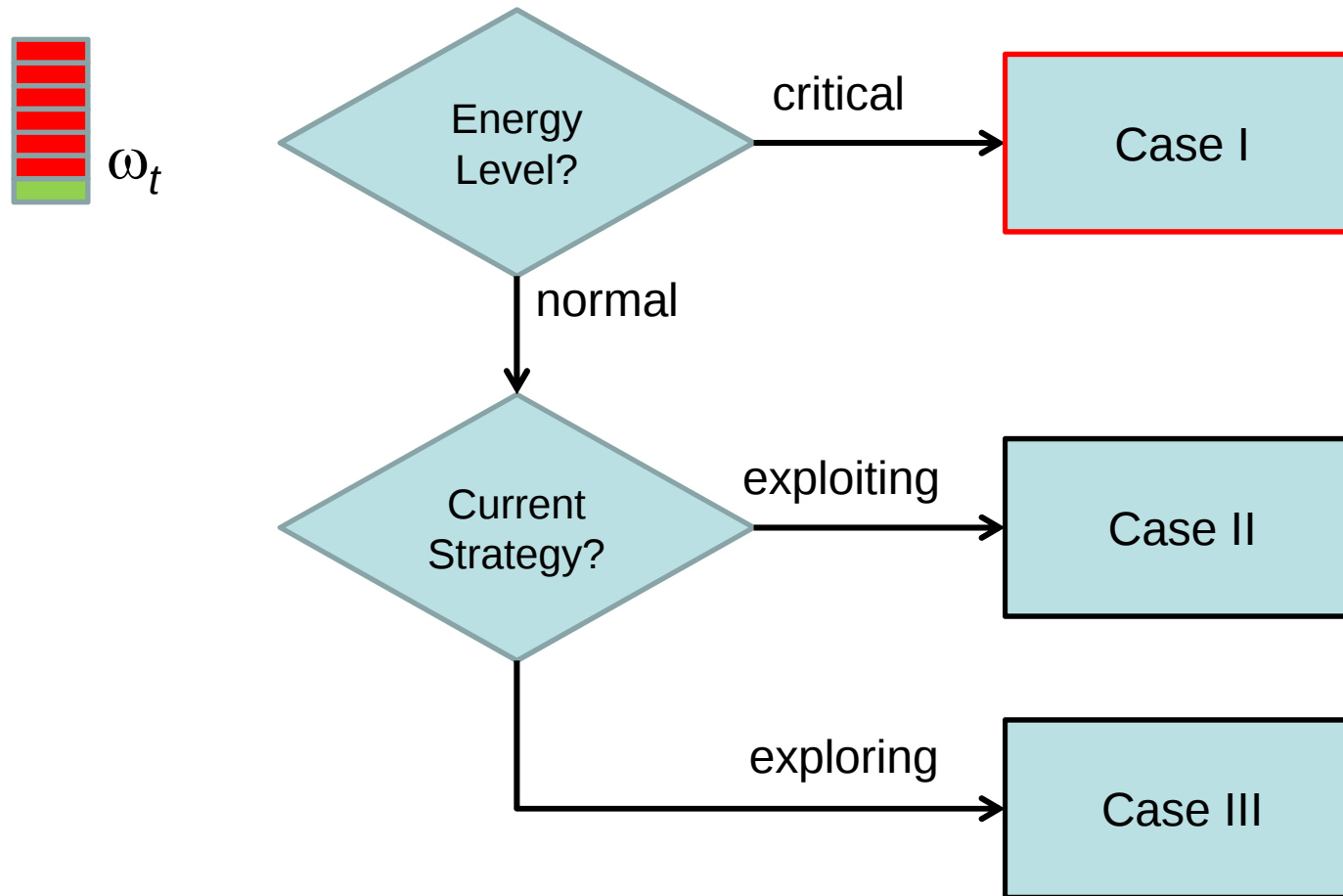


discount factor $\gamma = 0.9$

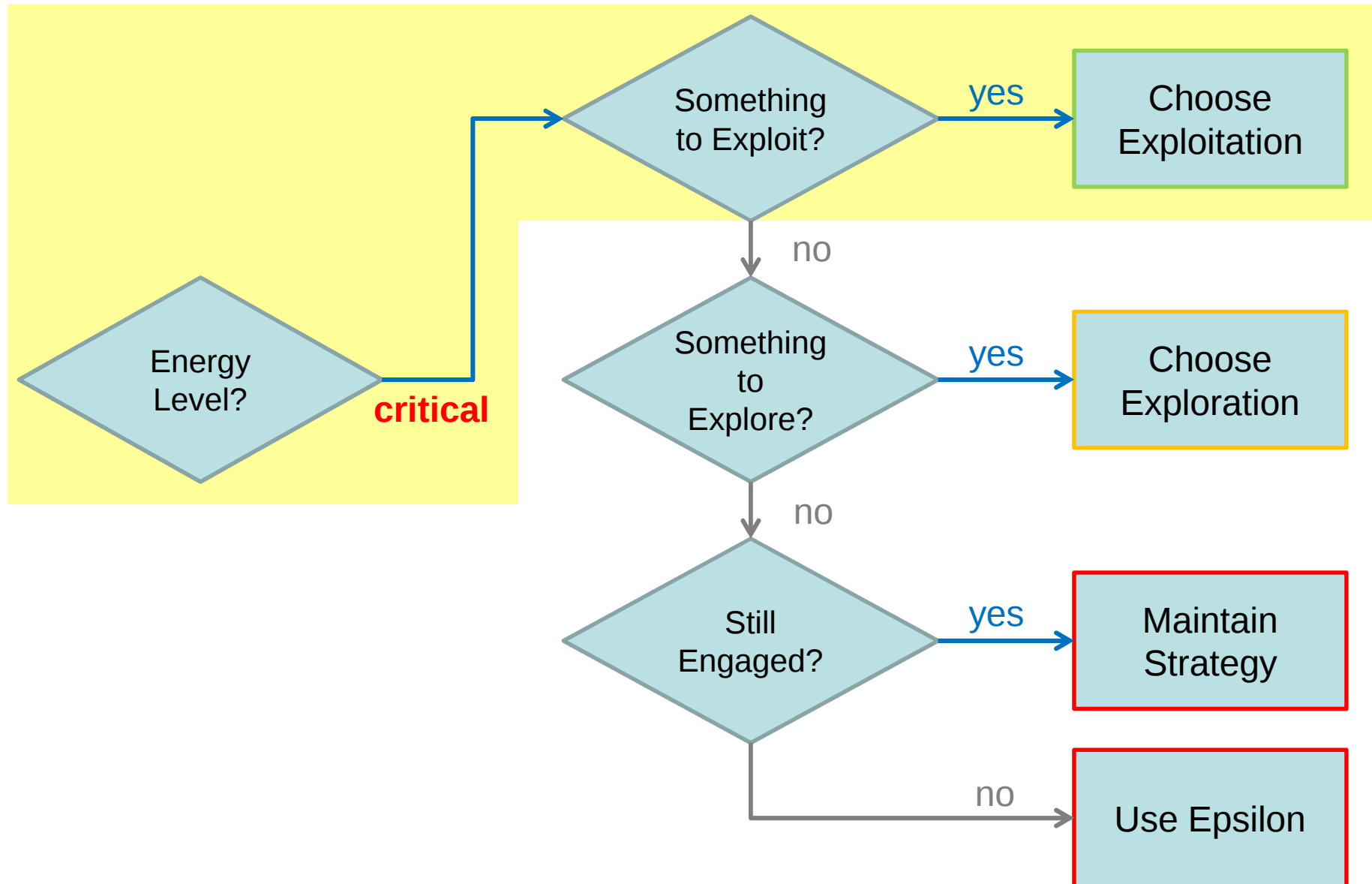
Utilities



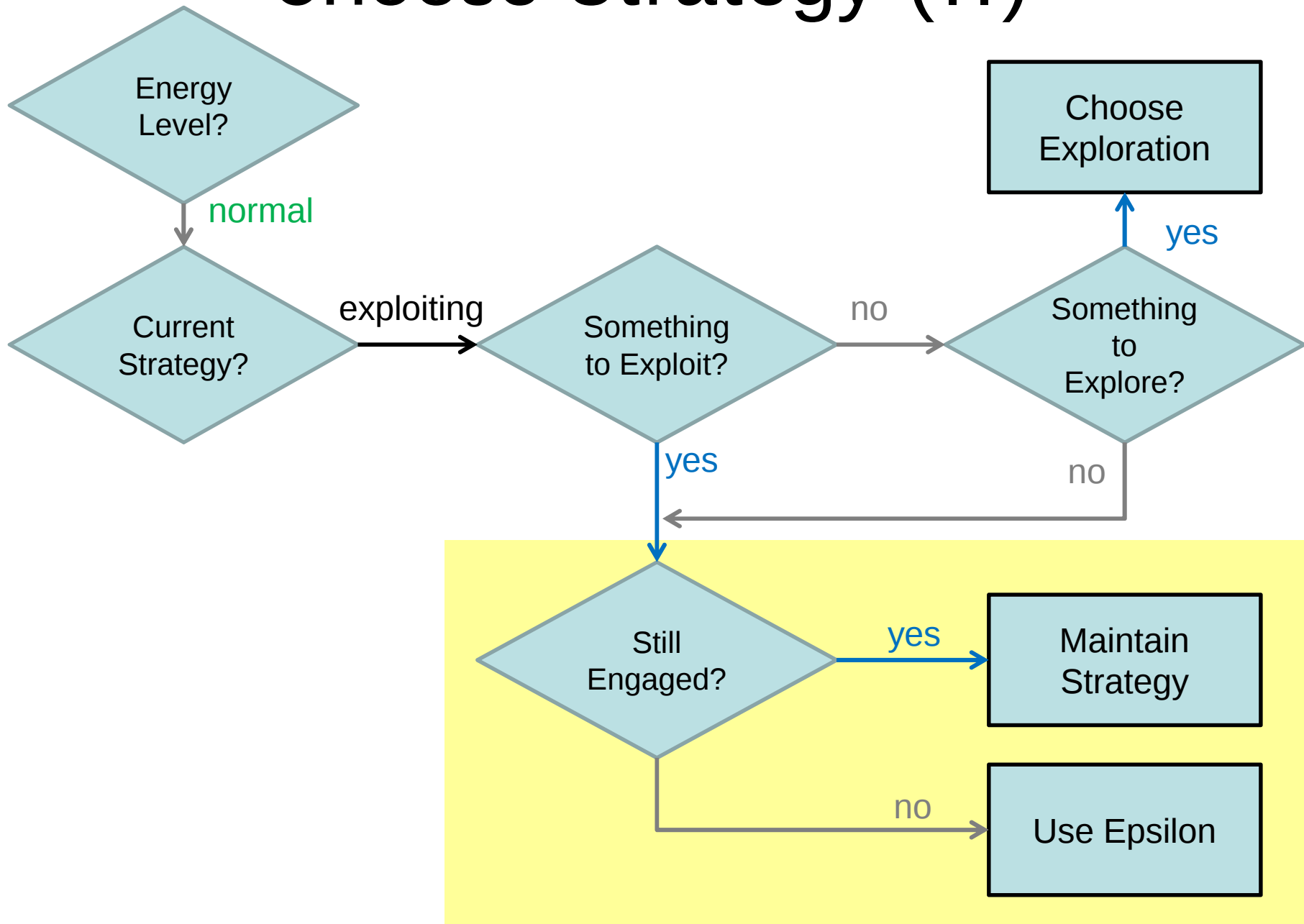
Choose Strategy (Engaged-Climber)



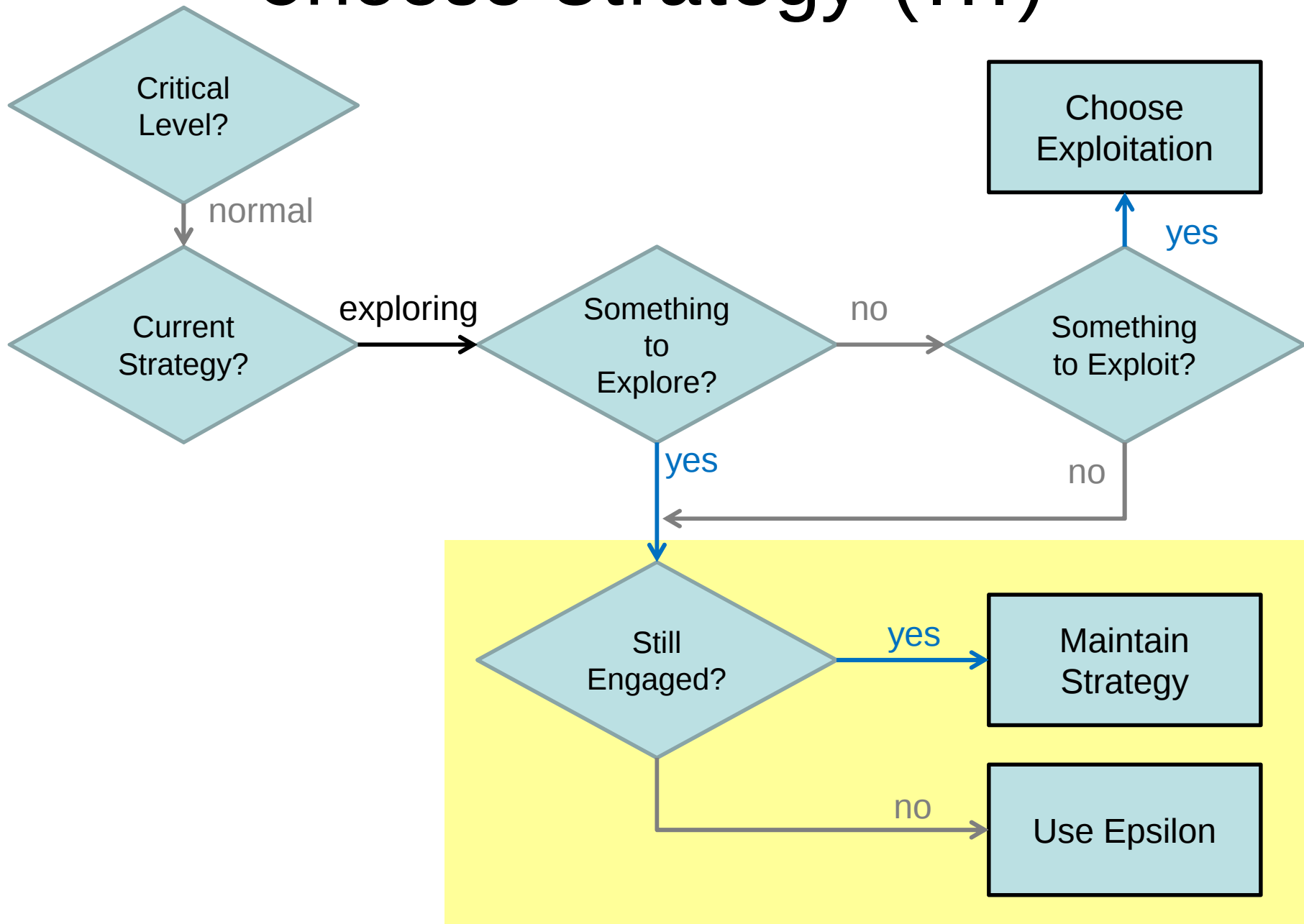
Choose Strategy (I)



Choose Strategy (II)

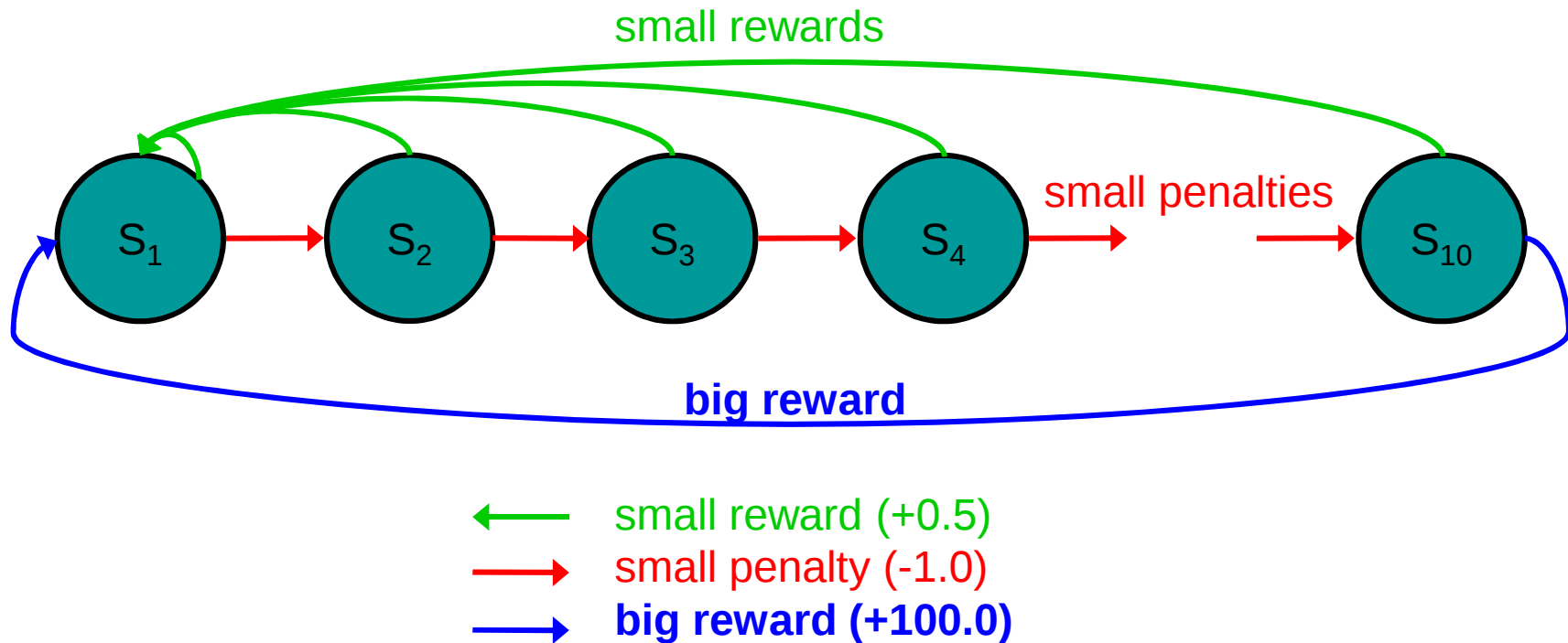


Choose Strategy (III)



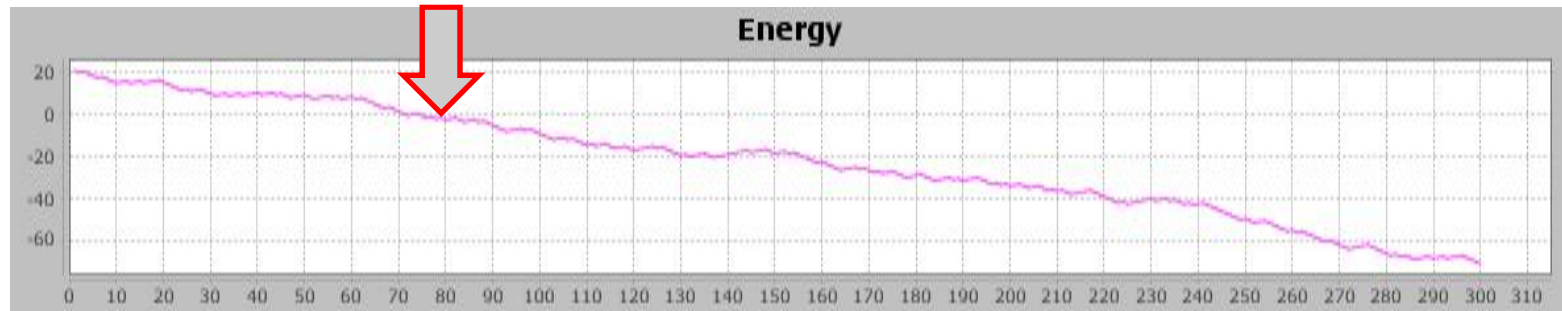
Experience : Chain States

- 10 states, 2 actions :
 - go forward
 - back to start

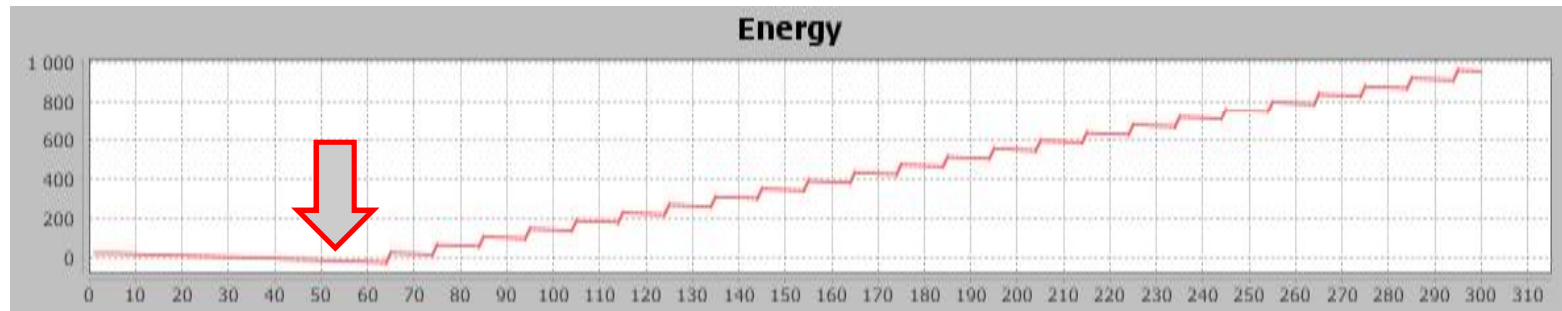


Experimental Results

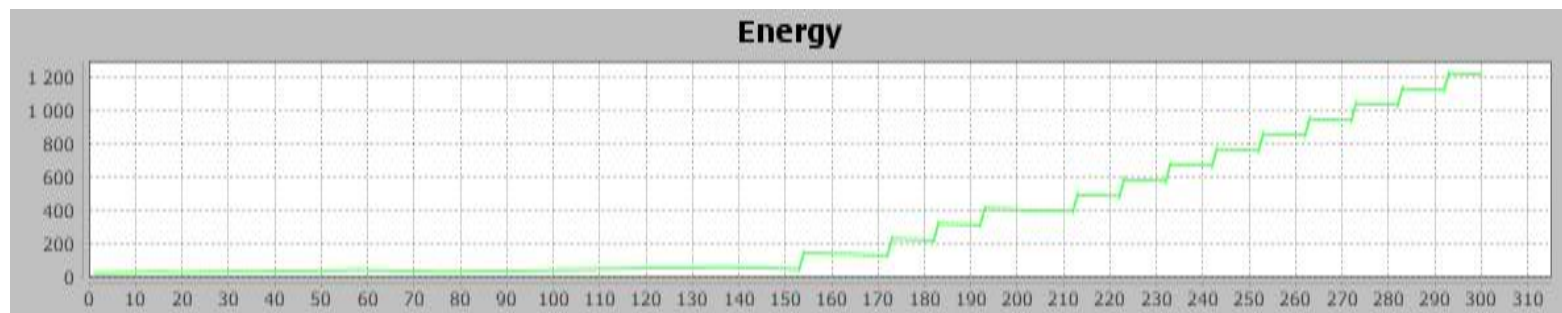
Eps



Opt



EC



Experimental Results

Table 1.: Experimental results

Method	Time to discover the goal	Minimum Score
ε -Greedy	≈ 1200	≈ -400
<i>Optimistic-Greedy</i>	≈ 60	≈ -30
<i>Engaged-Climber</i>	≈ 170	$\approx +10$

**using value-iteration method for calculating utilities*



Conclusions

- Curiosity
 - Policy for Exploring
 - Policy for Exploiting
- Engagement
 - More human-like behavior
- Consider limited resources



Perspectives

- Concrete search for peaks
- Factored Representations
- Partial Observation
- Multiple Policies
- Robustness



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